

# REORGANIZATION OF THE AUDITORY-PERCEPTUAL SPACE ACROSS THE HUMAN VOCAL RANGE

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## ABSTRACT

We investigated the auditory-perceptual space across a substantial portion of the human vocal range (220-1046 Hz) using multidimensional scaling analysis of cochlea-scaled spectra from 250-ms vowel segments. Three native German speakers produced vowels /i y e ø ε a o u/ (N=240) spanning a wide range of their respective voice frequency ranges, which were subsequently identified in a closed-set task by five phonetically trained listeners (>80% correct response). Our findings revealed systematic spectral alterations associated with vowel height and frontness as fundamental frequency increased and a distinct clustering around /i a u/ above 523 Hz. These results emphasize the importance of the overall spectral shape in vowel perception and demonstrate listeners' utilization of acoustic anchors at higher pitches. Moreover, this study sheds light on the quantal nature of these vowels and their potential impact on language evolution, offering a possible explanation for their widespread presence in the world's languages.

**Keywords:** auditory-perceptual space, fundamental frequency, pitch, vowels, quantal theory

## 1. INTRODUCTION

For much of the last century, it has been widely believed that vowels produced at high fundamental frequencies ( $f_0$ ) are challenging to comprehend, supported by numerous studies in the field of singing research (e.g., [1,2]). In 2013, Sundberg [3] provided a comprehensive overview, summarizing the results from various studies in the field of Western classical singing, and concluded that vowel recognition declines at an  $f_0$  of around 523 Hz (i.e., the musical note C5). Above this frequency, only the open vowels /a/ and /ɑ/ (i.e., the vowels with the highest  $F_1$ ) remain identifiable, while identification rates for all other vowels drop towards chance level at higher  $f_0$ . This outcome is expected due to the sparse distribution of harmonics at high  $f_0$ , leading to an undersampling of the vocal tract transfer function and, consequently, a less precise specification of the formant frequency distribution, a crucial acoustic representation in the vowel identification process.

Contrary to these findings, a few early studies outside Western classical singing showed accurate vowel identification at high  $f_0$  but did not consider secondary cues' impact [4,5]. Recent research has addressed these secondary cues at high  $f_0$ , such as vowel duration, formant transitions, and coarticulation (see [6,7,8] for more information on secondary cues). For example, Friedrichs et al. [9] found that the phonological function of the steady-state vowels /i y e ø ε a u o/ could be maintained at  $f_0$  up to 880 Hz in a two-alternative forced-choice task. By increasing the number of response options and talker variability, another study [10] demonstrated that the point vowels /i a u/ could even remain identifiable up to 1046 Hz. These findings align with those reported by Zhang et al. [11], who discovered that isolated vowels /i a u/ produced by a female Chinese Yue Opera singer could be identified with high accuracy up to around 932 Hz when presented to phonetically trained listeners in a free-choice identification task.

Considering the conflicting observations in singing research, it is possible that vowel recognition at high  $f_0$  is compromised by articulatory and acoustic adjustments made by classical Western Opera singers. Joliveau et al. [12] demonstrated, by measuring broadband acoustic excitation at the mouth of soprano singers, that they shift their first resonance frequency ( $f_{R1}$ ) towards  $f_0$  to increase vocal power in their performances. Such modifications were typically observed when  $f_0$  was high and approached  $f_{R1}$ . Altering the vocal tract's first resonance frequency may, therefore, significantly impact the perceived vowel category.

To date, little is known about the mechanisms that allowed vowel identification at very high  $f_0$  in the aforementioned studies outside Western classical singing. These mechanisms likely involve specific spectral properties and auditory-perceptual strategies employed by listeners [13]. In this study, we investigate the spectral properties of vowels within a range of 220 to 1046 Hz to explore the underlying auditory-perceptual mechanisms that drive the vowel identification process throughout the human vocal range. By examining these auditory-perceptual mechanisms and spectral properties, we aim to provide a better understanding of how vowel identification can be maintained at high  $f_0$  and the factors that contribute to the discrepancies observed

between Western classical singing and other singing styles. This knowledge can provide insights for researchers in singing, phonetics, and linguistics and contribute to the improvement of acoustic models for vowel recognition at high  $f_0$ .

## 2. METHOS

### 2.1. Participants

Five phonetically trained listeners (3 females, 2 males; mean age = 37.1 years, standard deviation = 8.4 years) participated in the listening experiment. All participants had audiometric thresholds of less than 20 dB hearing level at octave frequencies between 125 and 8000 Hz.

### 2.2 Stimuli

Three female native German speakers (mean age = 32.2, standard deviation: 2.5) with professional vocal training in singing or acting were selected from a corpus of 70 speakers [14] based on their extended vocal range and similar  $f_0$  in producing citation-form words and reading a story (mean 215.4 Hz, standard deviation 12.4 Hz). Recordings were made using a cardioid condenser microphone (Sennheiser MKH 40 P48) at a sampling frequency of 44.1 kHz and a constant distance of 30 cm from the speakers. The speakers produced the eight vowels /i y e ø ε a o u/ in isolation at ten target  $f_0$  ranging from 220 to 1046 Hz (i.e., 220, 330, 440, 523, 587, 698, 784, 880, 988, and 1046 Hz). The target  $f_0$  were played to the speakers as reference tones via studio monitor loudspeakers before each recording.  $f_0$  was measured with an autocorrelation method [15,16] in Praat [17] and manually checked. For each vowel, multiple recordings were made, and those with the closest distance to the target  $f_0$  (maximum deviation of 5%) were selected, resulting in a total of 240 vowels (10  $f_0$  x 8 vowels x 3 speakers). 250-ms segments were extracted from the vowel centers, normalized to an arbitrary intensity, and onset, and offsets were faded using raised cosines.

### 2.3. Procedure

The phonetically trained listeners participated in a multiple-choice transcription task in which they were presented with the stimuli vowels via closed headphones (Beyerdynamic DT 770 Pro, 250  $\Omega$ ) and asked to assign each vowel to one of the eight vowel categories displayed on a computer screen. Listeners could also assign the presented vowel to a category between two vowels (e.g., /i-ε/ instead of /i/ or /ε/). The output level could be chosen individually for comfort, and listeners were allowed to replay each

presented vowel multiple times. Only vowels with more than 80% correct responses were selected for subsequent analyses.

### 2.4. Cochlea-scaled spectra

Cochlea excitation patterns were simulated using a 200-channel linear gammatone filter bank, with bandwidths and center frequencies calculated using the ERB formulae by Glasberg and Moore [18]. The RMS level of the output wave was calculated and converted to dB for each filter channel. Frequency weighting was applied based on measurements made by Puria et al. [19] to account for the transmission properties of the middle ear.

### 2.5. Data analysis

Classical multidimensional scaling (MDS) analysis [20, 21] was performed on the cochlea-scaled spectra to model changes in the estimated auditory-perceptual space throughout the  $f_0$  range. MDS has been previously used to assess perceptual proximity or dissimilarity in vowels [22, 23]. At each target  $f_0$ , all eight vowels were assigned to specific coordinates in a two-dimensional space derived from the calculated distances of the cochlea-scaled spectra. The distances shown in the MDS space are linearly related to the spectral distance.

Considering a vowel clustering phenomenon at high  $f_0$  reported in previous studies [10,11], we aimed to investigate potential clustering of vowels at different  $f_0$  by calculating the Euclidean distances between vowel pairs that appeared to cluster together in the MDS space (cluster 1: /i e y/, cluster 2: /ø ε a/, cluster 3: /u o/). For each speaker and  $f_0$ , we calculated the Euclidean distance between normalized cochlea-scaled spectra of all vowel pairs within each cluster using the formula:

$$(1) \quad d(p, q) = \sqrt{\sum_i (q_i - p_i)^2}$$

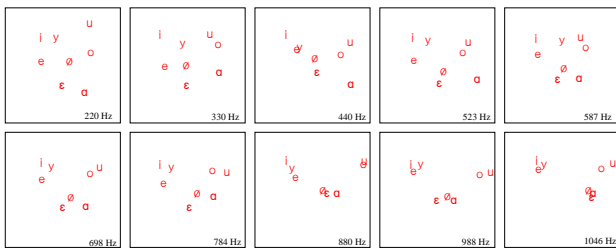
where  $d(p, q)$  is the Euclidean distance between two spectra, and  $p_i$  and  $q_i$  are the amplitude values at frequency bin  $i$  in spectra  $p$  and  $q$ , respectively. The summation is taken over all frequency bins  $i$  from the first to the last frequency bin in the spectra.

To assess the relationship between the  $f_0$  and the sum of Euclidean distances, we performed a piecewise mixed-effects linear regression with the Euclidean distances as the dependent variable and  $f_0$  as a fixed effect. Based on Sundberg (2013), which suggests that listeners' vowel identification performance decreases at around 523 Hz, the model allowed for different slopes in the relationship between  $f_0$  and the Euclidean distances, starting at 523 Hz. The random

effects in this model included the speaker and listener. This analysis helped us determine if the changes in the Euclidean distances were significantly different across the  $f_0$  range, providing insights into the clustering phenomenon and the underlying auditory-perceptual mechanisms involved throughout the human vocal range.

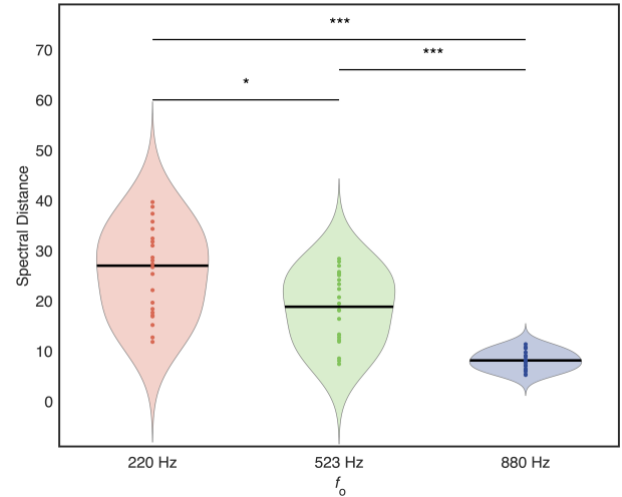
### 3. RESULTS

Fig. 1 displays the estimated auditory-perceptual space, averaged across the three speakers at all recorded frequencies between 220 and 1046 Hz. At the lowest  $f_0$  (220 Hz), the MDS space derived from cochlea-scaled spectra resembles a typical  $F_1$ – $F_2$  space. As the  $f_0$  increases, the vowel height dimension (vertical axis) partially collapses while the frontness dimension (horizontal axis) expands, altering the ratio of these dimensions from 1:1.44 (220 Hz) to 1:0.47 (1046 Hz). Despite this reorganization, the point vowels /i a u/ remain at the corners of the vowel space.



**Figure 1:** MDS plots showing the estimated auditory-perceptual space derived from cochlea-scaled spectra of the vowels used in this study throughout the  $f_0$  range from 220–1046 Hz (averaged across speakers). From around 523 Hz, the vowels start to cluster around the point vowels /i a u/.

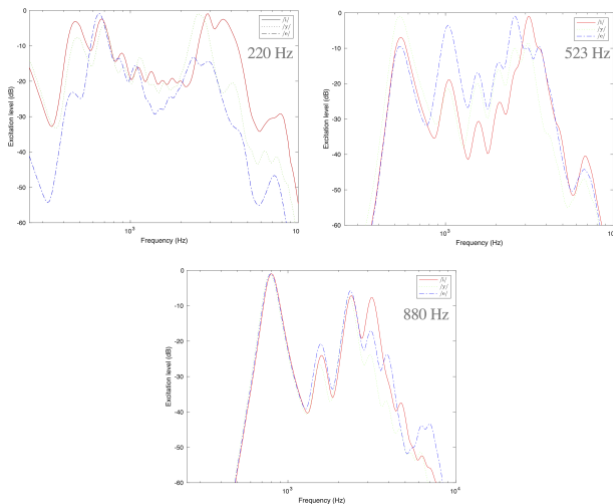
Starting around 523 Hz, shifts towards the categories /i a u/ are observed: /y e/ move towards /i/, /o/ towards /u/, and /ø ε/ towards /a/. Fig. 2 illustrates the average decrease in Euclidean distance measurements for vowels in these three clusters as  $f_0$  increases. Using the False Discovery Rate (FDR) controlling procedure [23], analyses of differences reveal no significant change in Euclidean distance measurements between the lowest  $f_0$  (220 Hz) and 330 Hz (adjusted  $p = 0.43$ ) as well as 440 Hz (adjusted  $p = 0.21$ ), but significant differences occur between 220 Hz and 523 Hz (adjusted  $p < .05$ ), as well as between 220 Hz and all  $f_0$  up to 784 Hz (all adjusted  $p < .05$ ) and up 1046 Hz (all adjusted  $p < .001$ ).



**Figure 2:** Violin plots showing the distribution of Euclidean distance measurements within the three clusters around the point vowels /i a u/ for a low, medium, and high  $f_0$ . The Euclidean distance between cochlea-scaled spectra decreases significantly towards the highest  $f_0$ .

Fig. 3 provides examples of cochlea-scaled spectra of /i y e/ forming a vowel cluster at high  $f_0$ . Dissimilarity is evident at the lowest  $f_0$  (220 Hz), but spectral proximity becomes more apparent at higher  $f_0$  (523 and 880 Hz). At 880 Hz, the Euclidean distance between the spectral vectors approaches the lower end of the scale and is only observable in high-frequency bands above 7 or 8 kHz.

Euclidean distances between the cochlea-scaled spectra of vowel pairs reveal a clear pattern across the investigated  $f_0$ . A piecewise linear mixed-effects regression with Euclidean distance as the dependent variable,  $f_0$  as a fixed effect (split at 523 Hz), and speaker and listener as random effects showed no significant relationship between  $f_0$  and Euclidean distance below 523 Hz ( $\beta_1 = -0.005$ ,  $p = 0.65$ ). At these lower  $f_0$ , the perceptual distance between vowels remains relatively constant. However, for  $f_0$  above 523 Hz, a significant negative relationship emerges between  $f_0$  and Euclidean distance ( $\beta_2 = -0.045$ ,  $p < .001$ ), suggesting that vowel clustering becomes more pronounced at higher  $f_0$ , with vowels becoming increasingly perceptually similar.



**Figure 3:** Cochlea-scaled spectra of the vowels /i y e/ produced by one speaker at fundamental frequencies of about 220, 523, and 880 Hz (top to bottom).

At the lowest  $f_0$  of 220 Hz, the median Euclidean distance was about 28 units, indicating a relatively large perceptual distance between vowels. As  $f_0$  increased up to 523 Hz, the median Euclidean distance remained relatively stable. From 523 Hz onwards, the median Euclidean distance gradually decreased, reaching a minimum of about 8 units at 880 Hz.

The two higher  $f_0$ , 988 Hz and 1046 Hz exhibited nearly identical median Euclidean distances as observed at 880 Hz ( $p > .05$ ), indicating that the vowel clustering phenomenon persists at these higher  $f_0$ . The piecewise linear mixed-effects regression also confirmed the lack of a significant difference in Euclidean distance between these three  $f_0$  ( $p > .05$ ). Overall, our results support the existence of a clustering phenomenon in vowel perception at higher  $f_0$ .

#### 4. DISCUSSION

The findings presented in this study suggest that the auditory-perceptual space undergoes a systematic reorganization throughout the human vocal range and a clustering phenomenon around the vowels /i a u/ at very high  $f_0$ . The patterns found in the MDS analysis likely allow vowels to remain distinguishable even when the vocal tract transfer function is undersampled to a high degree. Furthermore, this might explain why studies on vowel perception outside the field of Western Opera singing reported vowel intelligibility at high  $f_0$ .

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Our results indicate a tripartite organization of the auditory-perceptual space. At lower  $f_0$  (220–440 Hz), the arrangement of the vowels resembles that of a vowel quadrilateral or a typical  $F_1$ – $F_2$  space. This suggests that well-established mechanisms, such as processing formant frequency distributions, remain unaffected in this range. An auditory-perceptual reorganization begins at frequencies around 523 Hz, previously identified as the absolute frequency at which vowel intelligibility drops for all except /a/-like vowels [3]. This reorganization process evolves until around 880 Hz. From this  $f_0$  on (i.e., at 880, 988, and 1046 Hz), the auditory-perceptual clustering around the vowels /i a u/ is present, with three clusters formed by the vowels /i y e/, /ø ε a/, and /o u/. While accurate vowel category perception may be maintained between 523–880 Hz due to distinctive spectral patterns still observable at these frequencies, it seems unlikely that vowel perception can be as accurate at the three highest  $f_0$  due to spectral proximity within the clusters. However, it is probable that listeners can distinguish vowels between the three clusters up to the highest  $f_0$  humans are capable of producing. This finding may also have implications for the quantal theory of speech [25] and speech evolution theories, as it could shed further light on why these vowels can be found in almost all the world’s languages.

Several questions remain, however. The present study relied on five phonetically trained listeners who participated in the identification test and achieved an identification score of >80% for the selected vowels. Their phonetic expertise and the ability to replay a stimulus may have contributed to their performance. These listeners also made similar judgments on >30,000 vowels as part of creating a larger vowel and voice corpus [14,26,27]. Further studies would be necessary to determine the factors that helped them in the identification. Results from previous studies utilizing vowels from the same corpus and other sources are more consistent with the auditory-perceptual analyses presented here, as they also suggested a special role of the point vowels at high  $f_0$  [10,11,28]. These results propose that whole spectrum features may play an important role in vowel perception generally and that they provide a more comprehensive account than theories based solely on formant frequency patterns.

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